Remote Sensing Image Classification
Using Attribute Filters Defined over the Tree of Shapes

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Abstract—Remotely sensed images with very high spatial resolution provide a detailed representation of the surveyed scene with a geometrical resolution that at the present can be up to 30 cm (WorldView-3). A set of powerful image processing operators have been defined in the mathematical morphology framework. Among those, connected operators (e.g., attribute filters) have proven their effectiveness in processing very high resolution images. Attribute filters are based on attributes which can be efficiently implemented on tree-based image representations. In this work, we considered the definition of min, max, direct and subtractive filter rules for the computation of attribute filters over the tree of shapes representation. We study their performance on the classification of remotely sensed images. We compare the classification results over the tree of shapes with the results obtained when the same rules are applied on the component trees. The random forest is used as a baseline classifier and the experiments are conducted using multispectral data sets acquired by QuickBird and IKONOS sensors over urban areas.

Index Terms—Remote sensing, Classification, Mathematical Morphology, Tree of Shapes.

I. INTRODUCTION

REMOTE sensing instruments have been constantly improving their acquisition capabilities in terms of spatial resolution (e.g., WorldView-3: 0.3 m) and spectral information (e.g., AVIRIS: 224 spectral channels). Very High Resolution (VHR) remotely sensed images provide a precise and detailed representation of a surveyed scene. The spatial information contained in these images can be fundamental for any application which requires a detailed analysis of the scene.

Such detailed automatic analysis and interpretation can be achieved by using mathematical morphology, a theory on morphological transformations, which has provided a set of very powerful tools for image processing. It originates from the seminal works of Matheron and Serra who worked on problems in petrography and mineralogy [1–3]. Due to their pioneering work, mathematical morphology [4] [5] has achieved the status of a fundamental set of toolkit in image processing and analysis and has provided solutions to many tasks in different domains, such as remote sensing [6][7], pattern recognition [8][9] and medical imaging [10][11]. Morphological operators perform image analysis mainly at the pixel-level and the region-level. For instance an image can be processed by considering the values in the neighborhood of each pixel. Such neighborhood is defined by the extent of a spatial mask commonly referred to as a structuring element (SE) [12]. By varying the size and the shape of the SE, the image is probed by different spatial windows leading to different results that can provide useful information about the shape and size of the objects present in the image.

Recently, region-based filtering tools [13][14] (called connected operators) have received significant attention. Contrary to classical morphological operators (i.e., based on SEs), connected operators are edge preserving since they act directly on the connected components where the image is constant, the so-called flat zones. As a consequence, the characteristics of the spatial features are not distorted since the connected operators can remove boundaries between flat zones but cannot add new boundaries or modify existing ones. Connected operators are capable of performing image transformations that can selectively suppress some details from the image and maintain unaffected structures that are relevant for the analysis. However, the spatial information belonging to VHR images present heterogeneous characteristics, thus a multilevel analysis is required in order to perform a complete modeling.

For this purpose, the authors in [15] introduced morphological profiles (MPs). MPs are a multiscale decomposition of a grayscale image composed by stacking the filtered images obtained by transforming the input image with a sequence of opening and closing by reconstruction filters based on SEs. The operators by reconstruction permit to filter an image by entirely preserving the geometry of those structures that are not erased from the scene. In [16], the MPs were applied for the first time in a remote sensing classification task. Nevertheless, there are limitations on the capabilities of modeling the spatial information. In particular, the profiles built by the filters based on SEs are not able to easily model other features than the size of the objects.

Breen and Jones originally proposed morphological attribute filters (AFs) [17], which have received increasing attention...
filter rules have to be defined in order to generate the outputs of the filter. Several filtering approaches have been proposed in the literature such as min [13], max [24], viterbi [21] and direct [25]. The first three strategies belong to the class of pruning strategy (i.e., entire branches are removed), while direct is a non pruning strategy (i.e., isolated nodes might be deleted). The authors in [26] [27] later showed that the aforementioned filter rules may not offer the best possible strategy when filtering grayscale images with non increasing attributes. For instance, the regions that are not supposed to be deleted by the filter may disappear in the local background or be merged with adjacent regions. Consequently, they proposed the non pruning strategy subtractive, a new filter rule which can be efficiently used for shape decomposition. The above-mentioned rules have been proposed for dealing with min-tree and max-tree.

In this work, we considered the definition min, max, direct and subtractive for the computation of attribute filters over the tree of shapes. The hierarchy between its nodes is not driven by an ordering criterion of their graylevels (i.e., min-tree and max-tree), since the ordering follows the inclusion relationship of the regions. In such structure, the application of non pruning strategies is not straightforward. For instance, in the subtractive rule, the operation of updating the descendants over the tree of shapes can introduce new graylevels in the filtered images which were not present in the original image. We study the effect of the filtering rules by considering non increasing attributes, such as standard deviation and moment of inertia. We show that, according to the selected attributes and the filter rule, the characterization of the spatial information is performed differently. The sequential application of attribute filters over the component trees and the tree of shapes generates multi-level decompositions of the image which are called Attribute Profiles (APs) [28] and Self-Dual Attribute Profiles (SDAPs) [29], respectively. In this contribution we evaluate the classification accuracies obtained by applying APs and SDAPs generated by different filter rules. SDAPs already proved to be more effective than APs [29] for the increasing attribute area, since bright and dark regions are simultaneously processed. In [30], we have presented a preliminary comparison of the impact of different filter rules in the context of classification. Yet this comparison was performed on a single data set, and the description of those rules and their comparison were not complete. This paper aims at extending this analysis, by presenting a full and exhaustive comparison conducted using multispectral data sets acquired by QuickBird and IKONOS sensors over urban areas.

The remainder of the paper is structured as follows. Section II reviews morphological attribute filters computed on min-tree and max-tree and describes the filtering strategies in the context of increasing and non increasing operators. In Section III, we compute attribute filters with pruning and non pruning rules over the tree of shapes. The use of morphological attribute profiles in the context of classification of remotely sensed images is reviewed in Section IV. The experimental analysis, which includes the description of the data sets, the setup and the results, is given in section V. Section VI concludes this work with some remarks and hints at future research directions.
II. Attribute filters based on min and max tree

Attribute filters are morphological operators that perform a region processing since they act by merging regions of constant value, the so-called flat zones. Attribute filters can be efficiently implemented taking advantage of hierarchical representations of the image as a tree. In the following these representations will be introduced along with the implementation of the filtering techniques based on the min-tree and max-tree.

A. Min and Max tree

Let $f$ be a discrete two-dimensional grayscale image, then its spatial domain $E$ is a set of positions which map into a set of scalar values $V, f : E \rightarrow V$ with typically $E \subseteq \mathbb{Z}^2$ and $V \subseteq \mathbb{Z}$. A flat zone of $f$ is a region of connected pixels $CC_v(f)$ (connected component) of the level set $H_v(f) = \{x \in E, f(x) = v\}$, with $v \in V$. At each gray level, there may be multiple connected components $CC_k^v(f)$, with $k$ being some index variable. A peak component can be defined as the $k$th connected component $CC_k^v(f)$ of the lower $L(f)$ and upper $U(f)$ threshold sets as [31]:

\[
L(f) = \{x \in E, f(x) < v\},
\]

\[
U(f) = \{x \in E, f(x) \geq v\},
\]

There is an inclusion relationship between the peak components extracted by $L(f)$ and $U(f)$ which allows to associate a node of a tree $N_k^v(f)$ to the subset of $CC_k^v(f)$ with a fixed graylevel $v$ and represent the image as an hierarchical structure. The min-tree and max-tree structures represent the components in $L(f)$ and $U(f)$ respectively with their inclusion relations. The min-tree models the inclusion of regions according to the ordering graylevel criterion ($\leq$), thus the tree contains only the shapes that are darker than their neighborhood (i.e., the graylevel of each region is lower than their neighborhood graylevel). The root of the min-tree is the entire image domain at the greatest grayscale value, while the leaves are the regional minima. The max-tree is dual, and it contains only the regions that are brighter than the graylevel of their neighboring pixels. In this case the root is the whole image at the lowest grayscale and leaves are the regional maxima. Component trees are widely used for computing attribute filters [17] [27], pattern spectra [27] [32], and multi-scale decompositions [33]. In [34] a complete comparison of the different algorithms proposed in the literature (sequential and parallel) for their computation is detailed.

B. Increasing and Non increasing operators

Once the tree representation has been created, the filtering step analyzes each node by measuring a specific criterion and takes a decision on the elimination or preservation of the node. The simplification itself is governed by a criterion (e.g., a binary predicate $P$) that may involve simple notions such as size, contrast, or more complex ones such as texture, motion, or even criteria close to semantic notions, such as similarity to predefined shapes. Taking as a reference the predicate $P = \alpha(N_k^v(f)) \geq \lambda$, an attribute $\alpha$ is computed over each node $N_k^v(f)$ and if it does not satisfy the predicate different strategies as remove/preserve decisions can be used [27]. According to the type of criteria (e.g., predicate) and the property of the attribute, the resulting operator can be defined as increasing or non increasing.

In the context of a tree structure, this characteristic is related to the criterion assessed for each node. When the predicate is in the form $P = \alpha(N_k^v(f)) \geq \lambda$ or $P = \alpha(N_k^v(f)) \leq \lambda$ and the attribute is increasing (i.e., the attribute of a node can never be less than the values of its descendants in the tree), the operator is also increasing. In this case, as shown in Fig. 2(b), there is no problem in defining a level where the criterion is higher or lower than a given $\lambda$ threshold. Contrarily, when the attribute is not increasing (i.e. the attribute of a node can be less than the values of its descendants in the tree), any predicate leads to a non increasing operation. In particular, as shown in Fig. 2(c), the criterion sequence fluctuates around the $\lambda$ threshold and defining the set of nodes to remove is less straightforward.

![Fig. 2: Example of attribute values sequences for the nodes marked in red of the tree branch (a). Increasing attribute area (b), and non-increasing attribute moment of inertia (c). The attribute values sequence is marked are red, while the threshold imposed by the predicate $P$ is marked in blue.](image)

C. Connected operators: attribute filters

In this work we use a specific category of connected operators called attribute filters. When attribute filters are applied over the tree representation of an image, the operator leads to a pruning of the tree by removing the nodes whose associated regions do not fulfill $P$.

Two general approaches might be used at this point: pruning and non pruning strategies. In the former, a single cut is made along each path from leaf to root, and all nodes leaf-side of the cut are collapsed onto the highest surviving ancestor. In the second class of rules, the simplification of the tree is not limited to the removal of entire branches but also isolated nodes might be removed along a root path. For example, when a node is deleted, the value of the pixels belonging to the node are updated to the value of its oldest surviving ancestor. Different approaches can be used for dealing with non increasing attributes. For example, the Viterbi algorithm [21] addresses the decision of removing or preserving a node as an optimization problem, while in [35] the authors apply the filtering on a graph whose nodes are weighted with an increasing order by the attribute.

In the following section, a description of pruning and non pruning strategies is provided by including the pseudo-code of
the algorithms (a complete analysis can be found in [21] and [27]).

D. Pruning strategy

Pruning strategies consist in removing whole branches of the tree. They are simple to apply when the attribute is increasing since all nodes on which the criterion is not verified are organized in entire branches (i.e., if a node has to be removed, all of its descendants also have to be removed). When nodes of a branch are deleted, the level (i.e., graylevel) of their pixels are assigned to the level of the highest ancestor which satisfies the criterion.

The min rule prunes the branches from the leaves up to the last node that has to be removed. Therefore a node is removed if the predicate is false or if one of its ancestors is removed. The function Min rule (Algorithm 1) scans the tree starting from the root, and deletes a node when it does not satisfy the predicate or when its parent has to be removed.

The max rule cuts out the branches from the leaves up to the first node that has to be preserved. Thus, a node has to be removed if the predicate is false and all of its descendant nodes are deleted as well. In this case, the function Max rule (Algorithm 2) scans the tree starting from the leaves, and removes a node only when itself and its parent do not satisfy the predicate.

E. Non pruning strategy

A different type of image decomposition can be used in order to characterize heterogeneous regions and objects. The extraction of the pattern spectra [27] can be useful if the types of the details of interest are characterized by shape rather than size. This idea has been formalized as the so-called shape filters [26], and the operators which are anti-extensive and idempotent are not necessarily increasing. One example is the region perimeter: if a node \( N^k_i(f) \) is included in region \( N^k_j(f) \), no specific relation can be stated about their respective values. Non pruning strategies provide solutions for such cases where the simplification approach is not straightforward (i.e., the descendants of a node to be removed have not necessarily been removed).

Algorithm 1 Min rule

```
1: procedure MIN(tree, image, P)
2:     all nodes ← mark false
3:     for all nodes (from root to leafs) do
4:         if mark(parent)=true or P(node)=false then
5:             level(node) ← level(parent)
6:         node ← mark true
```

The direct rule consists simply in removing the nodes that do not fulfill the criterion. Thus, a node is removed if the predicate is false; its pixels are assigned to the graylevel of the highest ancestor which meets the criterion and its descendants are left unaffected (Algorithm 3). It has been proven in the literature that the direct rule is not the best strategy to deal with object enhancement and image decomposition based on shape [26]. The reason is that this strategy may lead to a loss of the contrast between the local background and the surviving descendant regions. The consequence, which is shown in [26], is that the difference between the original image and the filtered image may contain structures that meet the aforementioned criterion (further details will be explained in the next section).

In order to solve the previous issues, the authors in [26] proposed the subtractive rule, as a simple and consistent approach for non increasing attributes. The first part of the algorithm performs the same as the direct rule, meaning that the nodes that do not satisfy the predicate are removed. Afterwards, the deletion of a node triggers a propagation process, which updates the graylevel of the surviving descendant nodes, so that the contrast with the local background remains invariant. Algorithm 4 shows that, for each descendant node, firstly, its value is set to the minimum, and then, by considering all graylevels in turn, a unit term is added every time the algorithm finds a connected component which satisfies the predicate and contains the considered node. A dual analysis can be done in the case of a min-tree, where first the maximum value is assigned and then a unit term is subtracted for each node which satisfies the previous requirements.

Algorithm 2 Max rule

```
1: procedure MAX(tree, image, P)
2:     all nodes ← mark false
3:     for all nodes (from leafs to root) do
4:         if mark(node)=false then
5:             parent ← mark true
6:     if P(node)=true then
7:         node ← mark true
8:         parent ← mark true
9:     for all nodes (from root to leafs) do
10:        if mark(node)=true then
11:            level(node) ← level(parent)
```

Algorithm 3 Direct rule

```
1: procedure DIRECT(tree, image, P)
2:     for all nodes (from root to leafs) do
3:         if P(node)=false then
4:             level(node) ← level(parent)
```

Algorithm 4 Subtractive component tree rule

```
1: procedure SUBTRACTION (tree, image, P)
2:     for all nodes (from root to leafs) do
3:         if P(node)=false then
4:             UPDATE_DESCENDANTS(tree, node, P)
5:     function UPDATE_DESCENDANTS (tree, node, P)
6:         for all the descendants do
7:             level(descendant) ← min graylevel(tree)
8:             for all the graylevels considers each region do
9:                 if P(region)=true and region ⊆ node then
10:                    level(descendant) ← level(descendant) + 1
```
The algorithm computes the tree of shapes with quasi-linear time complexity when data quantization is low (typically 12 bits or less) and it works for nD images. Moreover, Crozet et al. [38] presented the first parallel algorithm to compute the morphological tree of shapes based on the previous algorithm [37]. The tree of shapes is a more general representation of the image with respect to the min-tree and max-tree and it has many advantages.

An example of tree of shapes computation (i.e., region growing) is shown in Fig. 3 (f). The FLST algorithm extracts each branch of the tree starting from the leaves and growing them up to the root until only a single flat region is reached. It comprehends both the $\mathcal{L}(f)$ and $\mathcal{U}(f)$ sets, and intrinsically eliminates the redundancy of information contained in those sets. Min-tree and max-tree are representations of the image, and usually not all the connected components present in $\mathcal{L}(f)$ are also present in $\mathcal{U}(f)$ and vice versa. Since the tree of shapes is self-dual, it makes no assumption about the contrast of objects (either light object over dark background or the contrary). Finally, it encodes the spatial inclusion of $\mathcal{CC}_k^S(f)$ in gray-level images so it is complementary to some other representations that focus on component (or region) adjacency.

### III. Attribute Filters Based on Tree of Shapes

Pruning and non pruning strategies have been proposed for the min-tree and max-tree representations. In this section, we consider pruning and non pruning filter rules for the computation of attribute filters over the tree of shapes. We show that the definition of \textit{min, max, direct} is equivalent to the case of component trees. We propose a different definition for the \textit{subtractive} rule, since the principle that regulates the hierarchy of the nodes in the tree of shapes follows the inclusion of different structures.

#### A. Tree of shapes

A self-dual tree has been defined in [23], called the tree of shapes (also known as inclusion tree), that describes the image $f$ contents in a unique way; such a tree can be interpreted as the result of merging the min- and a max-tree of the same image. The tree of shapes is a morphological self-dual representation of the $\mathcal{CC}_k^S(f)$ within an image (i.e., zones enclosed by an isolevel line). It was firstly introduced by Monasse et al. [23], where the structure was computed with the Fast Level Line Transform (FLLT) algorithm: it first computes the pair of dual component trees and then obtains the tree of shapes by merging both trees. Afterwards, Caselles et al. [31] introduced the Fast Level Set Transform algorithm (FLST), which relies on a region-growing approach to decompose the image into shapes. An operation called saturation is applied to the connected components which gives flat regions obtained by progressively merging nested regions. Specifically, the algorithm extracts each branch of the tree starting from the leaves and growing them up to the root until only a single flat region is reached. Song et al. [36], proposed to retrieve the tree of shapes by building the tree of level lines and exploiting its interior of each level line. Recently Geraud et al. [37] proposed a new algorithm to compute the tree of shapes in order to reduce the computational complexity and overcome the restriction to only 2D images of the previous methods. The algorithm computes the tree of shapes with quasi-linear order to reduce the computational complexity and overcome the restriction to only 2D images of the previous methods.

#### B. Increasing attributes

When the attribute is increasing, the filtering is straightforward and it consists of removing whole branches of the tree. In particular, all the filtering rules (i.e., pruning and non pruning) lead to the same filtering result [30]. However, in [29] it was shown that the use of the tree of shapes as a structure representing the image allows simultaneously to access the information present on both min-tree and max-tree. Moreover, the self-dual connected operators $\rho^S$ that are computed on the tree of shapes produce a greater simplification of the image with respect to non dual filters, since they operate simultaneously on the bright and dark components. An example of an attribute filter computed on the tree of shapes representation with the increasing attribute area is shown in Fig. 4. The self-dual operator $\rho^S$ is able to remove directly both bright and dark small structures [see the difference image.
Fig. 4: Attribute filtering of the grayscale image \( f \) in Fig. 3(a) using the area attribute with \( P = \alpha(C)C \leq 20 \). (a) Tree of shapes (nodes marked in red are removed). (b) Filtered image \( \rho^p(f) \) and (c) difference image \( f - \rho^p(f) \).

\[ f - \rho^p(f) \text{ Fig. 4(c)}, \] and it leads to a complete simplification of the image [see the filtered image \( \rho^f(f) \) Fig. 4(b)].

C. Non increasing attributes

As already explained in the previous section, in order to handle the non increasing attributes, pruning and non pruning strategies have been proposed. The decision about the most suitable strategy depends mainly on the application (e.g., image filtering or decomposition). An intuitive requirement when decomposing an image \( f \) based on shape rather than size (e.g., moment of inertia) is that the difference between the image \( f \) and the filtered image \( \rho^f(f) \) is an image which should only contain structures that do not meet the \( P \) [26] (i.e., the regions which have been filtered out). It was shown that the pruning strategies can not satisfy this requirement. For example, in the branch of the tree of shapes shown in Fig. 5(a):

\[
(A)N_5 \rightarrow (D)N_0 \rightarrow (I)N_5,
\]

which means that only the node D has been removed (i.e., it does not satisfy \( P \)). In this case, there are no pruning strategies that can simultaneously retain A and I, while removing D (e.g., Fig. 5(c) min removes all the nodes A-D-I, while Fig. 5(d) max preserves the whole branch). Furthermore, the authors in [26] proved that also the non pruning strategies such as direct may not perform efficiently. For example, the difference image shown in Fig. 5(e) contains regions which satisfy \( P \) (e.g., the nodes F-G-I-N).

The authors in [27] proposed a new strategy for non increasing attributes called subtractive rule, in order to address the previous issues. However, its definition was formulated for the max-tree structure for which the inclusion of the nodes is driven by grayscale rules. For instance, the definition of subtractive can not be directly applied to the tree of shapes. Particularly, in Algorithm 4 the updating process is achieved by considering all the graylevels in turn starting from the minimum (i.e., max-tree). This approach would make no sense in the tree of shapes structure since the hierarchy between the nodes follows the inclusion relationship of the regions. We propose here a different approach, where the intensity of each descendant node is lowered by the same amount of which the deleted node was lowered. The proposed subtractive function (Algorithm 5) begins with a loop where, for each node, starting from the leafs, a \( \Delta \) value is stored. The \( \Delta \) is equal to the \( \Delta \) of its parent. If the \( P \) of the node is false, a new value is added to \( \Delta \), equals to the difference between the level of the node and the level of its parent. Finally, for each node, \( \Delta \) is used to lower all the sub-components level of the surviving descendants nodes.

In this scenario, for the branch of the tree of shapes previously considered, the attribute filter removes the nodes D and updates the grayscale of the surviving descendant I. The filter first computes \( \Delta \) and then it updates the level of the node I as follows:

\[
\Delta = (A)N_5 - (D)N_0 = 5 - 0 = 5 \\
(I)N = (I)N_5 - \Delta = 5 - (-5) = 10
\]

The updating process solves the problem found in direct, where regions that satisfy \( P \) are lost in the filtered image since the contrast with the local background is not maintained. For example the surviving regions I and N do not appear in the filtered image with the direct rule in Fig. 5(e) while they are preserved by the subtractive rule in Fig. 5(f). This effect may become critical when filtering images representing objects in a real scene (i.e., remotely sensed images). For instance, the number of connected components within a filtered image with the direct rule can be much lower than the one contained in an image filtered with subtractive, which means that a part of the information related to the objects is lost. Finally, the updating of the graylevels of the descendants over the tree of shapes introduces new graylevels in the filtered image in Fig. 5(f), which were not present in the original image in Fig. 5(b).

IV. CLASSIFICATION WITH MORPHOLOGICAL ATTRIBUTE PROFILES

Attribute profiles (APs) were introduced in remote sensing in [39] as a sequential application of attribute filters based on a min-tree (i.e., attribute thickening operation \( \phi^T \)) and max-tree (i.e., attribute thinning operation \( \gamma^T \)). The AP is obtained by filtering an image \( f \) with attribute operators using a predicate with increasing threshold values \( \{\lambda_k\}^L \):

\[
AP(f) = \{\phi^{T_{\lambda_L}}(f), \phi^{T_{\lambda_{L-1}}}(f), ..., f, ..., \gamma^{T_{\lambda_{L-1}}}(u), \gamma^{T_{\lambda_{L}}}(f)\}
\]

with \( \phi \) and \( \gamma \) being the thickening and thinning operators based on the predicate \( T \), respectively, and \( T_{\lambda} \) a set of \( L \) ordered predicates.

Algorithm 5 Subtractive tree of shapes rule

1: procedure Subtractive (tree, image, \( P \))
2: \hspace{1cm} all \( \Delta(\text{node}) \leftarrow 0 \)
3: \hspace{1cm} for all nodes (from root to leafs) do
4: \hspace{2cm} \( \Delta(\text{node}) \leftarrow \Delta(\text{parent}) \)
5: \hspace{2cm} if \( P(\text{node}) = \text{false} \) then
6: \hspace{3cm} \( \Delta(\text{node}) \leftarrow \Delta(\text{node}) + \text{level(\text{node}) - level(\text{parent})} \)
7: \hspace{2cm} for all nodes (from root to leafs) do
8: \hspace{3cm} \text{level(\text{node}) = level(\text{node}) - \Delta(\text{node})}
APs provide a multilevel characterization of the spatial features which can be useful for the classification of very high resolution remote sensing images [29].

The Self-Dual Attribute Profiles (SDAPs) [29], were proposed as a version of the APs based on self-dual connected operators ρ dup, computed on the tree of shapes instead of considering a min-tree or max-tree. The use of the tree of shapes as a structure representing the image allows simultaneously to access the information present on the component trees. Moreover, the self-dual connected operators that are computed on the tree of shapes produce a greater simplification of the image with respect to non-dual filters, since they operate simultaneously on bright and dark components of the image. SDAPs is obtained by filtering an image f with attribute operators using a predicate with increasing threshold values:

\[ SDAP(f) = \{ f, \rho^{T_1}(f), \ldots, \rho^{T_{N-1}}(f), \rho^{T_N}(f) \} \] (4)

with ρ being the self-dual operator based on the predicate T, and T a set of L ordered predicates.

Dalla Mura et al. in [40] proposed Extended Attribute Profiles (EAPs) as the application of APs to hyperspectral data. An EAP is obtained by concatenating the APs (i.e., based on a single attribute) built on several feature components (FCs) extracted by a reduction technique (i.e., PCA) computed on the hyperspectral image. Thus, the EAP can be formally defined as:

\[ EAP = \{ AP(FC_1), AP(FC_2), \ldots, AP(FC_N) \} \] (5)

Analogously to the definition of EAP, Extended Self-Dual Attribute Profiles (ESDAPs) were proposed in [41]. They are generated by concatenating the SDAPs computed on different components. Each SDAP is built on one of the N features components extracted by a feature reduction transformation from a hyperspectral image:

\[ ESDAP = \{ SDAP(FC_1), SDAP(FC_2), \ldots, SDAP(FC_N) \} \] (6)

In contrast to APs, the SDAPs are composed of N + 1 images while APs, built with the same sequence of predicates are made up of 2N + 1 images.

V. EXPERIMENTAL RESULTS

The filtering strategies introduced in the previous section are highly relevant in any problem related with the identification of objects of different shape and structure on different scales. In this work we will illustrate their performance on the classification of remotely sensed images. Moreover, we provide the experimental results obtained by classifying stacks of filtered images generated by min, max, direct and subtractive filter rules applied over the tree of shapes representation (i.e., SDAP). We study the capability of those rules in extracting spatial information from a scene by considering different attributes. Additionally, we compare the performance of those rules in terms of classification accuracy by comparing their application to the min-tree and max-tree (i.e., AP).

A. Data set description and experimental setup

The first dataset used in our experiments is an image of Rome, Italy, acquired by the QuickBird satellite. The dataset consists of a low-resolution (2.4m) multispectral image with four bands Red, Green, Blue and Near Infrared and a high spatial resolution panchromatic image of 0.6m resolution. Fig. 6(a) shows the true-colour image while Fig. 6(b) shows the groundtruth data with the 9 classes available. The second dataset is an image of Reykjavik, Iceland, acquired by the IKONOS Earth imaging satellite. As with the other dataset, it consists of a low-resolution (4m) multispectral image with the four bands and a high spatial resolution panchromatic image of 1m resolution. A groundtruth dataset of 6 classes reported in Fig. 7(b) is available. For each dataset the panchromatic and multispectral images are pansharpened using the undecimated discrete wavelet transform (UDWT) method [42], and the obtained high-resolution multispectral images are used for the classification. For the experiments, the names of the different features used for the classification process will be referred hereinafter as follows:

1) PAN: panchromatic image.
2) AP: attribute profile built from the panchromatic image by using a specific attribute and filter rule.
3) SDAP: self-dual attribute profile built from the panchromatic image by using a specific attribute and filter rule.
4) MS+AP: stacked vector consisting of multispectral images (Red, Green, Blue and Infrared) and AP.
5) MS+SDAP: stacked vector consisting of MS and SDAP.

The attributes and the corresponding threshold values used for building APs and SDAPs are reported in Table. I(a) and Table I(b) for the Rome and Reykjavik data set respectively. The APs are computed by using the implementation of the min-tree and max-tree included in the C++ Milena library [43], while the SDAPs from an adaptation of the code for the tree of shapes provided in the MegaWave2 toolbox [44]. The number of trees of the RF classifier is 200, and all the other options are set with the default values. For each attribute, the table shows the classification result by considering different filtering rules and distinct features configuration. For example, each column (filter rule) of Table IV(a) consists of four different features configuration: AP (21 features), SDAP (11 features), MS (4 features) + AP (21 features) and MS (4 features) + SDAP (11 features). The classification experiments are repeated ten times, randomly selecting 10% of the references samples as training set, and the mean values of the overall (OA), average (AA) accuracy and kappa (K) coefficient are given.

B. Results

In the following subsections, we discuss the experimental results obtained for each attribute. Each table reports the classification accuracies for the features AP, SDAP, MS+AP and MS+SDAP. It is taken for granted that every time spectral features MS are added to the classifier, the resulting accuracies can only improve.
Fig. 5: Attribute filtering of the grayscale image $f$ (b), represented by the tree in (a), using moment of inertia with $P = \alpha(CC) \leq 0.22$ using pruning (min (c) and max (d)) and non pruning filtering strategies (direct (e) and subtractive (f)). Each column represents, from left to right, pruned tree, filtered image $\rho^p(f)$ and difference image $f - \rho^p(f)$.

1) **Area:** it belongs to the class of increasing attributes, thus each filter rule generate identical filtered images. In Table III we report the classification results for three feature stack compositions. The first column considers the features PAN and MS+PAN (i.e. the results are reported only for comparison purposes). The second and third columns report AP and SDAP respectively, which are built with the area attribute. When APs and SDAPs are classified, all the classes are detected with a higher precision since they carry a significant amount of geometrical information. The accuracies obtained by the SDAPs are slightly better than those achieved with the APs. In [29] it was already shown the effectiveness of SDAP based on the area attribute for the classification of a very high geometrical resolution scene.

2) **Standard deviation:** filters based on the non increasing attribute standard deviation perform a multilevel decomposition of the objects in the scene. Specifically, the simplification process is not related to the geometry of

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Thresholds</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area</td>
<td>25, 100, 500, 1000, 5000, 10000, 20000, 500000, 1000000</td>
</tr>
<tr>
<td>Standard Deviation</td>
<td>2.5, 5, 7.5, 10, 15, 20, 25, 30, 35, 40, 45, 50</td>
</tr>
<tr>
<td>Moment of Inertia</td>
<td>0.20, 0.25, 0.30, 0.35, 0.40, 0.45, 0.50, 0.55, 0.60, 0.65</td>
</tr>
</tbody>
</table>

TABLE I: Attribute threshold values for the profiles: (a) Rome and (b) Reykjavik data set.
the shapes but to the modeling of the homogeneity of the graylevels of the pixels belonging to the regions. We start the analysis by looking at the classification accuracies shown in Table IV and notice that the results for the different filter rules are comparable. Even if the standard deviation is a non increasing attribute, all the nodes belonging to a single branch of the tree may or not satisfy the predicate. This is because the attribute does not have a strong non increasing behavior. As a result, a filter which uses pruning and non pruning strategies will generate similar filtered images, and the profiles (i.e., APs or SDAPs) built on different rules will be very similar to each other.

3) Moment of Inertia: filters based on the non increasing attribute moment of inertia are able to discriminate the shape of different structures, since the attribute provides a measure related to the elongation of a region. Contrary to the standard deviation, the classification accuracies obtained with the different filter rules vary greatly to each other, as shown in Table V. This is due to the considerable non increasing trend along the tree branches of the attribute values, which lead each filter rule to decompose an image in a different way.

We consider each filter rule separately and we provide a detailed analysis for the attribute filters applied over the tree of shapes for the Rome data set (there is an exhaustive literature related to the use of pruning and non pruning strategies with min-tree and max-tree [27]). The graphs in Fig. 8 show the average values of the graylevels of the pixels within each class for each threshold of the moment of inertia attribute in the SDAPs generated by different filter rules. This is useful for understanding the response of each class through the different threshold values of the profile.

When considering the min rule, the filter produces a considerable simplification of the scene. Moreover, the presence of a node that does not fulfill the criterion close to the root of the tree produces the removal of entire branches. For example, the filter starts to remove almost all the regions at the threshold value $\lambda = 0.35$ as shown in Fig. 9(a). The plot of Fig. 8(a) indicates that the pixels belonging to the different classes get the same constant value for threshold values greater than $\lambda = 0.35$. The images within the profile which are filtered at those thresholds, do not carry any spatial information (i.e., no regions have survived), leading the classifier to achieve poor classification results in both datasets, as shown in Table V.

In the case of max rule, the filter might not perform any effective simplification of the scene leading to filtered images that can be similar to the original image for most part of the threshold set. The plot of Fig. 8(b), shows that the pixels within the classes maintain almost the same grayvalue for all the thresholds. For instance, the filtered image at the threshold value $\lambda = 0.35$ shown in Fig. 9(b) is not decomposed yet. As a consequence, the classification accuracies obtained with AP
and SDAP are similar, since the operator does not perform an effective filtering for the different thresholds (i.e., no structures are extracted).

Different considerations have to be done when the non pruning rules direct and subtractive are taken into account. As shown in Fig. 8(c) and 8(d) the pixel values of the different classes do not take the same constant value at a certain threshold as in the case of min rule. Moreover, contrary to the max rule, the change in the trend of each class is more visible along the thresholds. This is due to the spatial information represented by the surviving regions after the filtering with non pruning strategies. Looking at the classification results in Table V, SDAPs achieve greater classification results with the subtractive if compared with the direct rule. As discussed in section III, unlike the direct rule, when a node in the tree is deleted, the subtractive propagates new values to its surviving descendants. Consequently, the contrast grayvalue between regions that are not filtered out and the local background is preserved. An example of a subscene of the Rome data set filtered with direct and subtractive is shown in Fig. 10. The effect of the propagation can be seen in Table II, which reports the number of connected components within the filtered images with direct and subtractive rules at different threshold values. For each threshold value, the number of connected components after filtering with subtractive is always greater than the one obtained with direct. Regions that satisfy P may be lost in the filtered image with direct since the contrast with the local background is not maintained. Thus, the classifier can benefit from the spatial information brought by those additional regions. Subtractive can achieve better accuracy results as reported in Table V and provide more accurate classification maps as shown in Fig. 11. The difference between the considered filter rules in terms of CPU processing time is not relevant. The profiles AP and SDAP are computed in a few seconds only by the rules for both data sets on a computer having Intel(R) Core (TM) i7-4710HQ CPU 2.50 GHz and 16 GB of memory.

<table>
<thead>
<tr>
<th>threshold</th>
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<th>0.35</th>
<th>0.40</th>
<th>0.45</th>
<th>0.50</th>
<th>0.55</th>
<th>0.60</th>
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<tbody>
<tr>
<td>direct</td>
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<td>595934</td>
<td>432206</td>
<td>308832</td>
<td>264216</td>
<td>214108</td>
<td>181111</td>
<td>155237</td>
<td>132170</td>
<td>114753</td>
</tr>
<tr>
<td>subtractive</td>
<td>733759</td>
<td>559334</td>
<td>432206</td>
<td>308832</td>
<td>264216</td>
<td>214108</td>
<td>181111</td>
<td>155237</td>
<td>132170</td>
<td>114753</td>
</tr>
</tbody>
</table>

**Table II: The number of connected components within the filtered images with direct and subtractive rules and their difference number $|CC|_{sub} - |CC|_{direct}$ for each threshold values of moment of inertia.**

VI. CONCLUSIONS AND FUTURE LINES

Very high resolution remotely sensed imagery provides precise geometrical information. In this paper, mathematical morphology has been exploited for designing new operators able to filter hierarchical structures which represent an image. In this work, we considered the definition of the filter rules direct, max, min and subtractive for the computation of attribute filters over the tree of shapes representation. We generated a tree-based representation of the image, then filtered the representation and finally reconstructed the filtered image from the filtered tree. We showed that subtractive rule preserves contrast grayvalue between regions that are not filtered out and introduces new graylevels in the filtered images which were not present in the original image. We studied the performance of the different rules in terms of classification accuracy in the context of APs and SDAPs, by considering the non increasing attributes standard deviation and moment of inertia. We have proved that when the criterion presents a strong non increasing behavior (i.e., moment of inertia), attribute filters provide heterogeneous profiles for the different filtering strategies. In this case, by looking at the classification accuracies obtained in our experiments, one can conclude that subtractive is the most effective filter rule in our context. Contrary to that, we have shown that if the criterion is more similar to an increasing behavior (i.e., standard deviation), the different filter rules provide similar profiles. Finally, due to the properties of the tree of shapes, we have shown that SDAPs outperform APs in terms of classification accuracies. Although the acceptable time for generating the profiles, our future research aims to develop real-time implementations for large scenes on GPUs. We will work on a new algorithm implemented in parallel fashion in order to compute the tree of shapes and the different filter rules.

REFERENCES

TABLE III: Classification accuracies of (a) Rome and (b) Reykjavik data set (mean value with its standard deviation in brackets) obtained by the panchromatic and spectral features MS and the AP and SDAP based on the attribute area.

<table>
<thead>
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<tbody>
<tr>
<td>AA</td>
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<td>85.06 (0.12)</td>
<td><strong>87.34 (0.12)</strong></td>
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<tr>
<td>OA</td>
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<td><strong>88.04 (0.04)</strong></td>
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<tr>
<td>K</td>
<td>28.15 (0.14)</td>
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<td><strong>SDAP (15)</strong></td>
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<td><strong>95.18 (0.07)</strong></td>
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<tr>
<td>OA</td>
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<tr>
<td>K</td>
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<td>93.72 (0.04)</td>
<td><strong>94.72 (0.04)</strong></td>
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TABLE IV: Classification accuracies of (a) Rome and (b) Reykjavik data set (mean value with its standard deviation in bracket) for each filter rule. First, the spatial features APs and SDAPs are considered (non increasing attribute standard deviation). Finally, the spectral information MS is added as additional features. The number of features is reported in the parentheses.

<table>
<thead>
<tr>
<th></th>
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<td>K</td>
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<td></td>
<td><strong>SDAP (11)</strong></td>
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<td><strong>MS + SDAP (15)</strong></td>
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<tr>
<td>AA</td>
<td>85.96 (0.12)</td>
<td>84.86 (0.16)</td>
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</tr>
<tr>
<td>OA</td>
<td>85.64 (0.11)</td>
<td>84.12 (0.17)</td>
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</tr>
<tr>
<td>K</td>
<td>82.64 (0.13)</td>
<td>80.83 (0.21)</td>
<td>82.79 (0.14)</td>
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TABLE V: Classification accuracies of (a) Rome and (b) Reykjavik data set (mean value with its standard deviation in bracket) for each filter rule. First, the spatial features APs and SDAPs are considered (non increasing attribute moment of inertia). Finally, the spectral information MS is added as additional features. The number of features is reported in the parentheses.

<table>
<thead>
<tr>
<th></th>
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<th>AP (21)</th>
</tr>
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<td></td>
<td><strong>SDAP (11)</strong></td>
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<td><strong>MS + SDAP (15)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>AA</td>
<td>82.07 (0.04)</td>
<td>94.23 (0.05)</td>
<td>95.18 (0.07)</td>
<td></td>
<td></td>
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<tr>
<td>OA</td>
<td>87.50 (0.11)</td>
<td>94.26 (0.07)</td>
<td>93.07 (0.09)</td>
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<td></td>
</tr>
<tr>
<td>K</td>
<td>71.91 (0.14)</td>
<td>91.29 (0.06)</td>
<td>93.07 (0.09)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Fig. 11: Classification maps for the experiments reported in Table V(a) using a single training and test set: (a) SDAP with *min*, (b) SDAP with *max*, (c) SDAP with *direct*, (d) SDAP with *subtractive*, (e) MS+SDAP with *min*, (f) MS+SDAP with *max*, (g) MS+SDAP with *direct* and (h) MS+SDAP with *subtractive*. 

Notes in Computer Science (including subseries Lecture Notes in Artificial Intelligence and Lecture Notes in Bioinformatics), vol. 6671 LNCS, 2011, pp. 306–319.


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